# Verifying Solvers: How Much do You Want to Prove?

Mathias Fleury January 17, 2024



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 not all techniques can be represented by current proof formats

#### Program Verification This talk!

- works for every input, so no overhead
  - does not crash even if run the program for a year

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## Restrictions

 Parsing is always trusted CakeML has some modelisation of file systems, but don't try "grep aaa file >> file" at home

• Printing the answer is trusted too

- The resulting SAT solvers live outside of their system
  - you cannot use them in the system you do the proofs

## A Personal History of Solver Verification



incomplete especially because the bottom-up approach is a good master thesis

## A Personal History of Solver Verification



Fleury: functional code, DPLL, no restarts, propagation by going over all clauses, decision by going over all clauses. but it terminates and is complete Solves no problem from the SAT Comp

Skotåm: imperative code, CDCL, restarts, watch literals, decision heuristic. Solves > 150. Top: Some theory expressed in your toolBottom Some (hopefully fast) codeAll full verifications go top-down.seL4 kernel is mixed:Specification -> Haskell <- C</td>Most partial verifications go bottom-up.Most natural for each tool!

# Bottom-Up Or the Art of Proving very little

## Organisation



Translation from Rust to why3 (unverified) [Denis, Jourdan, Marché, ICFEM'21]

1' transalation from Guru to C [Stump et al, PLPV'09]

2': only used in a SAT checker

## Implicit Checker The checker = the verification

#### Every approach I am aware of: checker = resolution checker

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**Theorem (Correctness)** 

Deriving  $\perp$  implies that the problem is UNSAT.

Deriving the empty clause: input problem unsat
Conflicts on current level: runtime assertion
Termination: Unknown
No conflict+all assigned: checking of the model
No crash: depends on the approach

#### Well-behaved: no read past end of array

#### Clauses: not modified except by resolution

• But: non trivial for minimization where the resolution is implicit

Assume you already have a working CDCL.

Adding restarts means:

1. call backtrack to level 0

That is all

except for heuristics, performance debugging, ...

## What is hard?

 Usually relies on automatic provers, which must be able to handle the specification
 Skotåm: swapping literals

No termination

ITP don't like non-termination

Closer to programs written by hand easier to try different strategies

**Top-Down Approach: Proving Too much** 

## Organisation



mantics from 2'. Or Lammich: LLVM generation 1. trusted as trivial translation (SML generation)

**Theorem (Total Correctness**<sup>⊥</sup>) Deriving ⊥ iff the probem is UNSAT. No conflict + total assignment = SAT. Termination.

**Theorem (Total Correctness IsaSAT-LLVM)** If the answer is not unknown, it is either SAT with a model or UNSAT.

IsaSAT-SML had full correction SML semantics does not forbid arrays  $\ge 2^{64}$ , no compiler support

<sup>&</sup>lt;sup>1</sup>At some point, memory representation can cause also aborts.

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## **Refinement in IsaSAT**



Deriving the empty clause: unsat (OR: derive conflict at level 0) Conflicts on current level: completeness of propagations Termination: Yes IsaSAT can answer unknown if too many clauses  $\sum_{c \in clauses} 5 + |c| \approx |clause\_memory| \ge 2^{63}$ No crash: yes (up to the assumptions on memory) allocation does not fail Assume you already have a working CDCL.

Adding restarts means:

- change your CDCL (to include a counter to increase restart interval)
- 2. change the refinement to be based on the extended CDCL
- 3. add restarts with the counter. Make sure that it does not overflow.

That is all

except for heuristics, performance debugging, ...

## What is hard?

• you have to prove everything

lots of code

• limited by the speed of your tools bring Isabelle to its knee

 hard to find people Isabelle and code synthesis can be seen as two different systems

#### In retrospect over the entire project:

- Many components that <u>are not independent</u> everything is parametrized by the set of variables...
   Watch list can be indexed by every literal in the set of clauses
- Mistakes have been made: too much coupling ... that is not duplicated
   Better: watch lists are defined over a set of literals that is the
  - same as the set of clauses also moving up proof that index valid
- But: refactoring takes time.

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In retrospect over the entire project:

• Testing new features hard Some I implemented and proved things that did not work and I removed.

• Testing improvement for code generation structure was forced, not a choice. Pointers

## What Can You Not Express?

```
• aliasing
struct ISASAT {
    TRAIL trail;
    CLAUSES clauses; ....
};
struct ISASAT solver;
isasat->trail = assign(lit, solver->trail);
```

 pointers are complicated IsaSAT: I tried to use a pointer to a state and never managed to make it less than 10 times slower

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The Code

Solver	SAT	UNSAT
IsaSAT	175	130
Creusat	145	79
versat	60	62

#### Table 1: Results on the SC2015 according to Skotåm (24 GB, 1800 s)



many out-of-memory for CreuSAT



21/27 many out-of-memory for CreuSAT



21/27 many out-of-memory for CreuSAT

#### How Good Is The Code (I)? Guru

```
void * gpropagate_h(int gnv_24, int gdl_4, void * gas_37, void * gws_17) {
 start_gpropagate_h: {
/* match with exactly one case: gassign state */
void * gpa_13;
void * gwhy_6;
void * gdls 6;
void * ghist 6;
int ghist_cur_4;
int ghist end 4;
void * gcarraway tmp 119;
gpa_13 = ginit_unique_unique(guwarray, gas_37, ((gAssignState_gassign_state *)gas_37)->gpa_2)
gwhy 6 = ginit unique unique(gwarray, gas 37, ((gAssignState gassign state \star)gas 37)->gwhy 2)
gdls_6 = ginit_unique_unique(guwarray, gas_37, ((gAssignState_gassign_state *)gas_37)->gdls_2
ghist 6 = ginit unique unique(guwarray, gas 37, ((gAssignState gassign state *)gas 37)->ghist
switch ((int)gcarraway tmp 120) {
```

fprintf(stderr,"abort at /Users/kain/Projects/versat/old\_versions/0.6/src/unitprop.g, line 76

#### (If times permits)

HTML version of the Isabelle files: https://people.mpi-inf. mpg.de/~mfleury/IsaFoL/current/Weidenbach\_ Book/IsaSAT/IsaSAT\_Inner\_Propagation\_Defs. html#IsaSAT\_Inner\_Propagation\_Defs.unit\_ propagation\_update\_statistics|const

Correcntess theorem: https://people.mpi-inf.mpg.de/ ~mfleury/IsaFoL/current/Weidenbach\_Book/IsaSAT/ IsaSAT\_All\_LLVM.html

## How Good Is The Code (II)? IsaSAT

define ISASAT\_STATE @unit\_propagation\_outer\_loop\_wl\_D(ISASAT\_STATE %x) #0 {

```
start:
  %x1 = call i8 @IsaSAT_Profile_PROPAGATE ()
  call void @IsaSAT_Profile_LLVM_start_profile (i8 %x1)
  br label %while start
while_start:
 %s = phi ISASAT STATE [ %x3, %while body ], [ %x, %start ]
  %x2 = call i1 @literals_to_update_wl_empty_fast_code (ISASAT_STATE %s)
  br i1 %x2, label %while_body, label %while_end
while body:
  %xb = call { ISASAT_STATE, i32 } @select_and_remove_from_literals_to_update wl(ISASAT_STA
  %a1 = extractvalue { ISASAT STATE. i32 } %xb. 0
  %a2 = extractvalue { ISASAT STATE, i32 } %xb, 1
  %x3 = call ISASAT STATE @unit propagation inner loop wl D (i32 %a2, ISASAT STATE %a1)
  br label %while start
while end:
  %xc = call i8 @IsaSAT Profile PROPAGATE ()
  call void @IsaSAT Profile LLVM stop profile (i8 %xc)
  ret ISASAT STATE %s
```

(only edit: ISASAT\_STATE is unfolded in the code and remove prefix from function names)

## How Good Is The Code (II)? CreuSAT

```
#[cfg_attr(feature = "trust_unit", trusted)]
#[ensures(f.equisat(^f))]
pub fn unit_propagate(f: 8mut Formula, trail: 8mut Trail, watches: 8mut Watches) -> Result<()</pre>
    let mut i = trail.curr i;
    let old_trail: Ghost<&mut Trail> = ghost! { trail };
    let old f: Ghost<&mut Formula> = ghost! { f };
    let old_w: Ghost<&mut Watches> = ghost! { watches };
    while i < trail.trail.len() {</pre>
        let lit = trail.trail[i].lit;
        match propagate_literal(f, trail, watches, lit) {
             Ok() => {}
             Err(cref) => {
                 return Err(cref);
        i += 1:
    trail.curr i = i;
    0k(())
```

(only edit: remove some invariants and ensures)

## Conclusion

## Comparison: How different are there really?

 Removing assertions from bottom-up means being more top-down and requires more proofs where automation struggles

Very hard to remove proofs from top-down

 Link top-down with concrete code? Currently has not been tried but I am trying to find a student

## Conclusion

- Only application of verified SAT solvers: finishing last at SAT Competition, getting Masters, or PhDs
- Unexpectedly, IsaSAT correlates the least with Kissat on SC2022
   benchmarks
   observation by Max Heisinger
- But: do you have applications where proof checking is not possible?
- What is the right timeout for the SAT Competition? In 2023: 5000 s solving + 9 × 5000 s checking. with 5× in total, probably still behind Laurent, but not last