

# Bounded Model Checking and CBMC

Armin Biere, Alessandro Cimatti, Edmund Clarke  
Daniel Kröning, Flavio Lerda, Yunshan Zhu

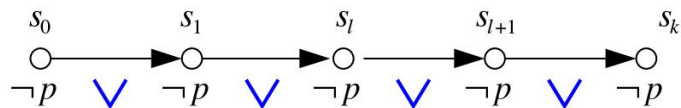
CAV Award 2018

Oxford, UK  
June 15th, 2018

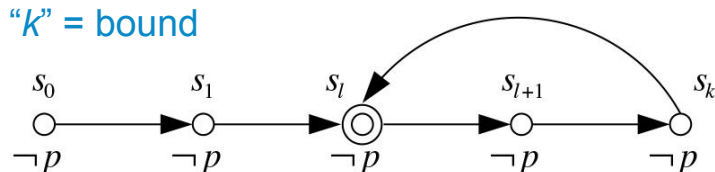
# Bounded Model Checking

[BiereCimattiClarkeZhu'1999]

- look only for counter example made of  $k$  states



or



- simple for *safety properties*

$p$  invariantly true

$$I(s_0) \wedge T(s_0, s_1) \wedge \dots \wedge T(s_{k-1}, s_k) \wedge \bigvee_{i=0}^k \neg p(s_i)$$

- harder for *liveness properties*

$p$  eventually true

$$I(s_0) \wedge T(s_0, s_1) \wedge \dots \wedge T(s_{k-1}, s_k) \wedge \bigwedge_{i=0}^k \neg p(s_i) \wedge \bigvee_{l=0}^k T(s_k, s_l)$$

- compute and bound  $k$  by diameter

# How did Bounded Model Checking happen?

- 1997: interest and capacity of BDDs stalled but there were success stories of “other” techniques  
CAV’97 in Haifa had an invited talk by *Arne Borälv* on  
“The Industrial Success of Verification Tools Based on Stålmarck's Method”
- *Edmund Clarke* hired *Yunshan Zhu* and *Armin Biere* as Post-Docs with the job-description  
***Use SAT for Symbolic Model Checking!*** (YZ expert on Theorem Proving, AB on BDDs)
- struggled for 10 months to come up with something that could replace / improve on BDDs  
mainly looked at *QBF* back then (point was that we need to handle quantifiers to do image computation)
- *Alessandro Cimatti* came to an AI conference in Pittsburg and at lunch (at an Indian Restaurant)  
we realized, that for planning they **do not care about completeness**  
*What if we apply this to model checking?*      *How to handle temporal logic?*
- after one afternoon for the theory and 3 months of implementation, benchmarking, writing it up ...

# Symbolic Model Checking without BDDs\*

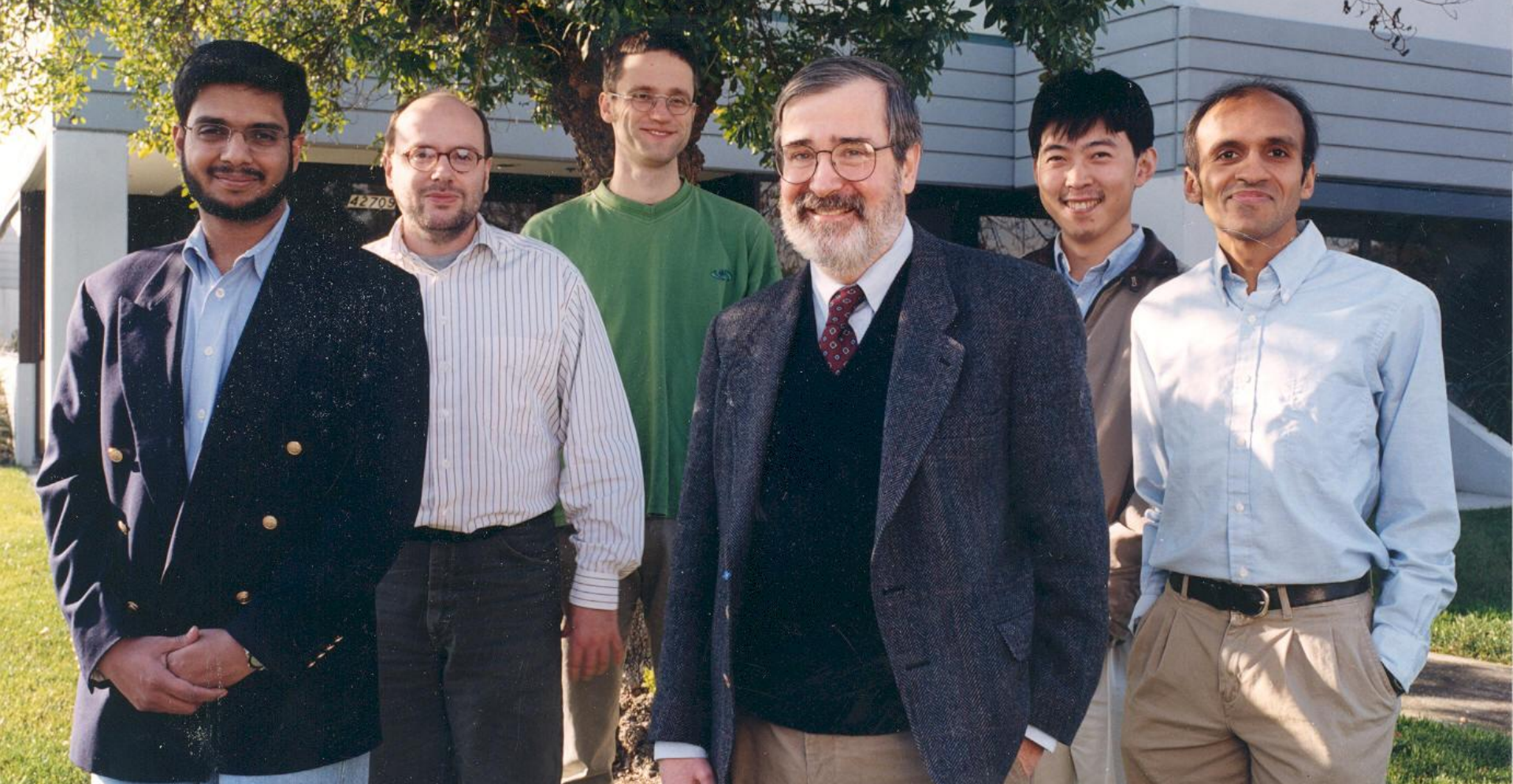
Armin Biere<sup>1</sup>, Alessandro Cimatti<sup>2</sup>, Edmund Clarke<sup>1</sup>, and Yunshan Zhu<sup>1</sup>

<sup>1</sup> Computer Science Department, Carnegie Mellon University  
5000 Forbes Avenue, Pittsburgh, PA 15213, U.S.A

{Armin.Biere, Edmund.Clarke, Yunshan.Zhu}@cs.cmu.edu

<sup>2</sup> Istituto per la Ricerca Scientifica e Tecnologica (IRST)  
via Sommarive 18, 38055 Povo (TN), Italy  
cimatti@irst.itc.it

**Abstract.** Symbolic Model Checking [3, 14] has proven to be a powerful technique for the verification of reactive systems. BDDs [2] have traditionally been used as a symbolic representation of the system. In this paper we show how boolean decision procedures, like Stålmarck's Method [16] or the Davis & Putnam Procedure [7], can replace BDDs. This new technique avoids the space blow up of BDDs, generates counterexamples much faster, and sometimes speeds up the verification. In addition, it produces counterexamples of minimal length. We introduce a *bounded model checking* procedure for LTL which reduces model checking to propositional satisfiability. We show that bounded LTL model checking can be done without a tableau construction. We have implemented a model checker **BMC**, based on bounded model checking, and preliminary results are presented.





Authors Armin Biere, Alessandro Cimatti, Edmund Clarke, Yunshan Zhu

Publication date 1999/3/22

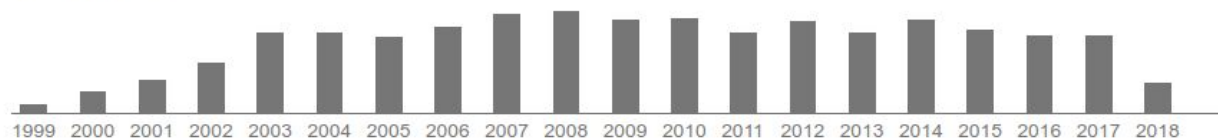
Conference International conference on tools and algorithms for the construction and analysis of systems

Pages 193-207

Publisher Springer, Berlin, Heidelberg

Description Abstract Symbolic Model Checking [3],[14] has proven to be a powerful technique for the verification of reactive systems. BDDs [2] have traditionally been used as a symbolic representation of the system. In this paper we show how boolean decision procedures, like Stålmarck's Method [16] or the Davis & Putnam Procedure [7], can replace BDDs. This new technique avoids the space blow up of BDDs, generates counterexamples much faster, and sometimes speeds up the verification. In addition, it produces counterexamples of minimal length. We introduce a bounded model checking procedure for LTL which reduces model checking to propositional satisfiability. We show that bounded LTL model checking can be done without a tableau construction. We have implemented a model checker BMC, based on bounded model checking, and preliminary results are presented.

Total citations [Cited by 2495](#)



Source: Google Scholar, 28th June 2018

Authors Armin Biere, Alessandro Cimatti, Edmund M Clarke, Masahiro Fujita, Yunshan Zhu

Publication date 1999/6/1

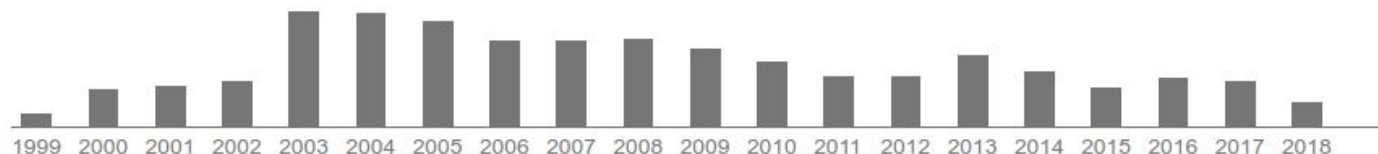
Conference Proceedings of the 36th annual ACM/IEEE Design Automation Conference

Pages 317-320

Publisher ACM

Description In this paper, we study the application of propositional decision procedures in hardware verification. In particular, we apply bounded model checking, as introduced in [1], to equivalence and invariant checking. We present several optimizations that reduce the size of generated propositional formulas. In many instances, our SAT-based approach can significantly outperform BDD-based approaches. We observe that SAT-based techniques are particularly efficient in detecting errors in both combinational and sequential designs.

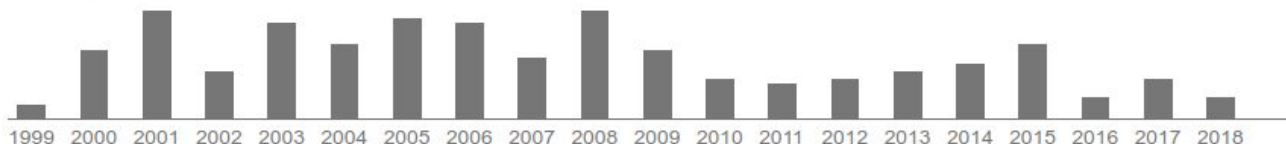
Total citations [Cited by 863](#)



Source: Google Scholar, 28th June 2018

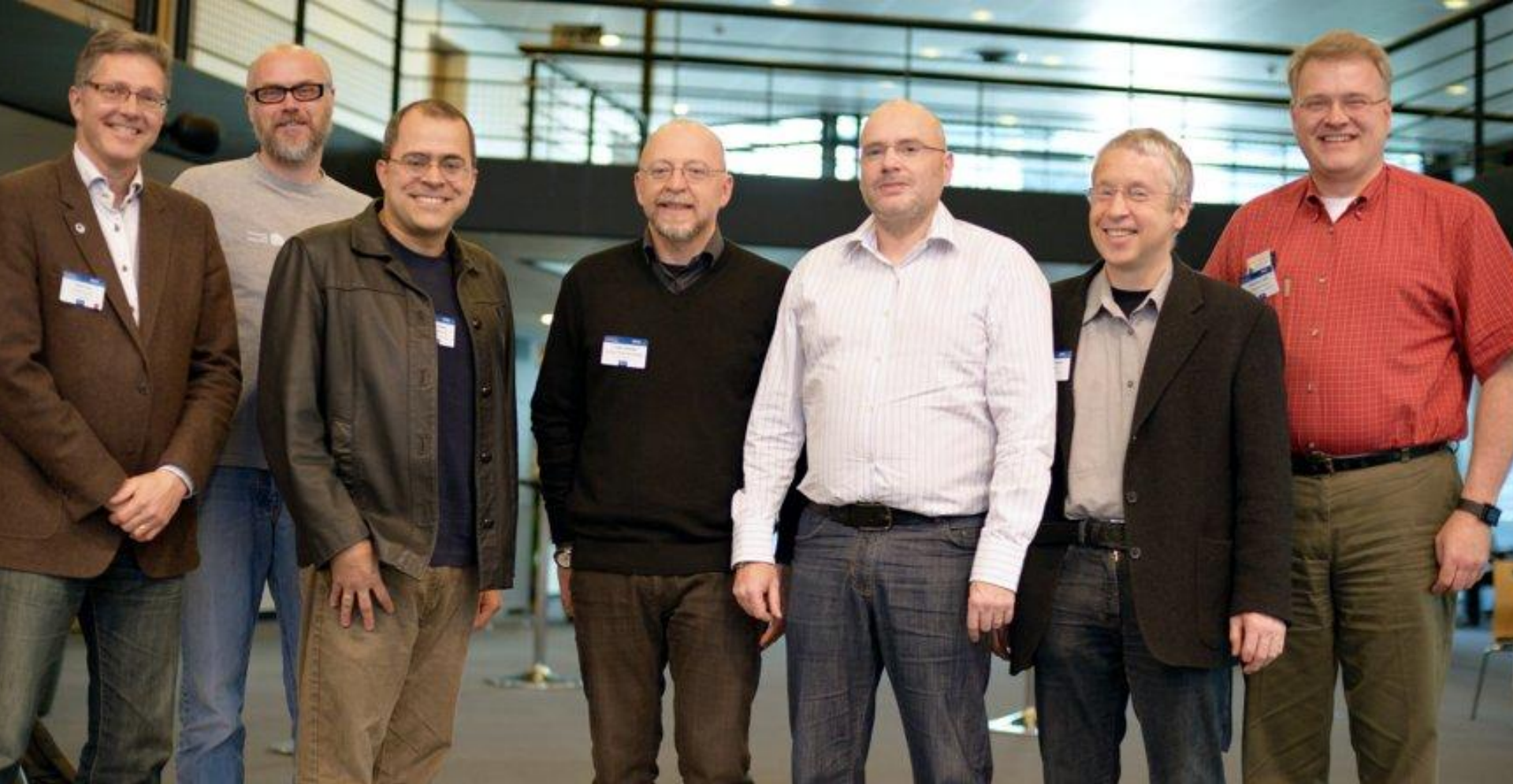
## BMC

Authors	Armin Biere, Edmund Clarke, Richard Raimi, Yunshan Zhu
Publication date	1999/7/6
Conference	International Conference on Computer Aided Verification
Pages	60-71
Publisher	Springer, Berlin, Heidelberg
Description	Abstract In [1] Bounded Model Checking with the aid of satisfiability solving (SAT) was introduced as an alternative to symbolic model checking with BDDs. In this paper we show how bounded model checking can take advantage of specialized optimizations. We present a bounded version of the cone of influence reduction. We have successfully applied this idea in checking safety properties of a PowerPC microprocessor at Motorola's Somerset PowerPC design center. Based on that experience, we propose a verification methodology that we feel can bring model checking into the mainstream of industrial chip design.
Total citations	Cited by 180



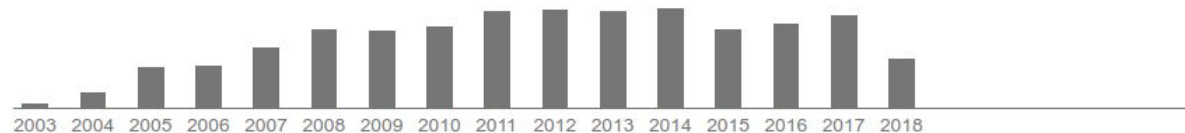
Source: Google Scholar, 28th June 2018





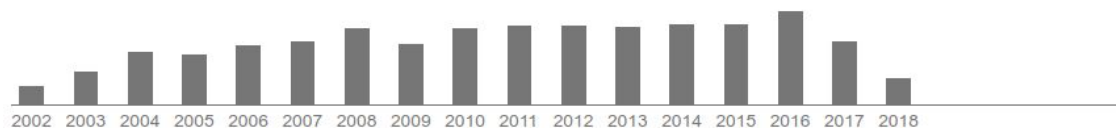
# BMC

Authors	Armin Biere, Alessandro Cimatti, Edmund M Clarke, Ofer Strichman, Yunshan Zhu
Publication date	2003/12
Journal	Advances in computers
Volume	58
Issue	11
Pages	117-148
Description	Symbolic model checking with Binary Decision Diagrams (BDDs) has been successfully used in the last decade for formally verifying finite state systems such as sequential circuits and protocols. Since its introduction in the beginning of the 90's, it has been integrated in the quality assurance process of several major hardware companies. The main bottleneck of this method is that BDDs may grow exponentially, and hence the amount of available memory restricts the size of circuits that can be verified efficiently. In this article we survey a technique called Bounded Model Checking (BMC), which uses a propositional SAT solver rather than BDD manipulation techniques. Since its introduction in 1999, BMC has been well received by the industry. It can find many logical errors in complex systems that can not be handled by competing techniques, and is therefore widely perceived as a complementary ...
Total citations	<a href="#">Cited by 857</a>



Source: Google Scholar, 28th June 2018

Authors	Edmund Clarke, Armin Biere, Richard Raimi, Yunshan Zhu
Publication date	2001/7/1
Journal	Formal methods in system design
Volume	19
Issue	1
Pages	7-34
Publisher	Kluwer Academic Publishers
Description	<p>The phrase model checking refers to algorithms for exploring the state space of a transition system to determine if it obeys a specification of its intended behavior. These algorithms can perform exhaustive verification in a highly automatic manner, and, thus, have attracted much interest in industry. Model checking programs are now being commercially marketed. However, model checking has been held back by the state explosion problem, which is the problem that the number of states in a system grows exponentially in the number of system components. Much research has been devoted to ameliorating this problem. In this tutorial, we first give a brief overview of the history of model checking to date, and then focus on recent techniques that combine model checking with satisfiability solving. These techniques, known as bounded model checking, do a very fast exploration of the state space, and for ...</p>
Total citations	<a href="#">Cited by 700</a>



Source: Google Scholar, 28th June 2018

# BMC



# Replacing Testing with Formal Verification in Intel® Core™ i7 Processor Execution Engine Validation

Roope Kaivola, Rajnish Ghughal, Naren Narasimhan, Amber Telfer,  
Jesse Whittemore, Sudhindra Pandav, Anna Slobodová, Christopher Taylor,  
Vladimir Frolov, Erik Reeber, and Armaghan Naik

Intel Corporation, JF4-451, 2111 NE 25th Avenue, Hillsboro, OR 97124, USA

**Abstract.** Formal verification of arithmetic datapaths has been part of the established methodology for most Intel processor designs over the last years, usually in the role of supplementing more traditional coverage oriented testing activities. For the recent Intel® Core™ i7 design we took a step further and used formal verification as the primary validation vehicle for the core execution cluster, the component responsible for the functional behaviour of all microinstructions. We applied symbolic simulation based formal verification techniques for full datapath, control and state validation for the cluster, and dropped coverage driven testing entirely. The project, involving some twenty person years of verification work, is one of the most ambitious formal verification efforts in the hardware industry to date. Our experiences show that under the right circumstances, full formal verification of a design component is a feasible, industrially viable and competitive validation approach.

## 1 Introduction

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Material

## 6 Formal Verification Value Proposition

The conventional wisdom about formal verification in industrial context is easy to spell out: it is a costly and time-consuming activity that is often seen as a necessary evil. However, the value proposition of formal verification is not always clear. In this paper, we explore the value proposition of formal verification in the context of industrial design and testing.

Formal verification (FV) is a technique for proving the correctness of a design against a set of requirements. It is a rigorous method that can be used to verify the correctness of a design against a set of requirements.

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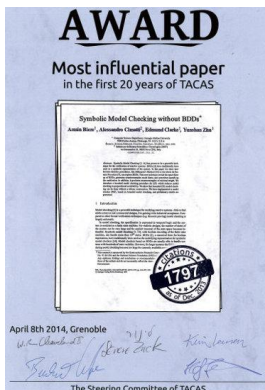
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# Impact

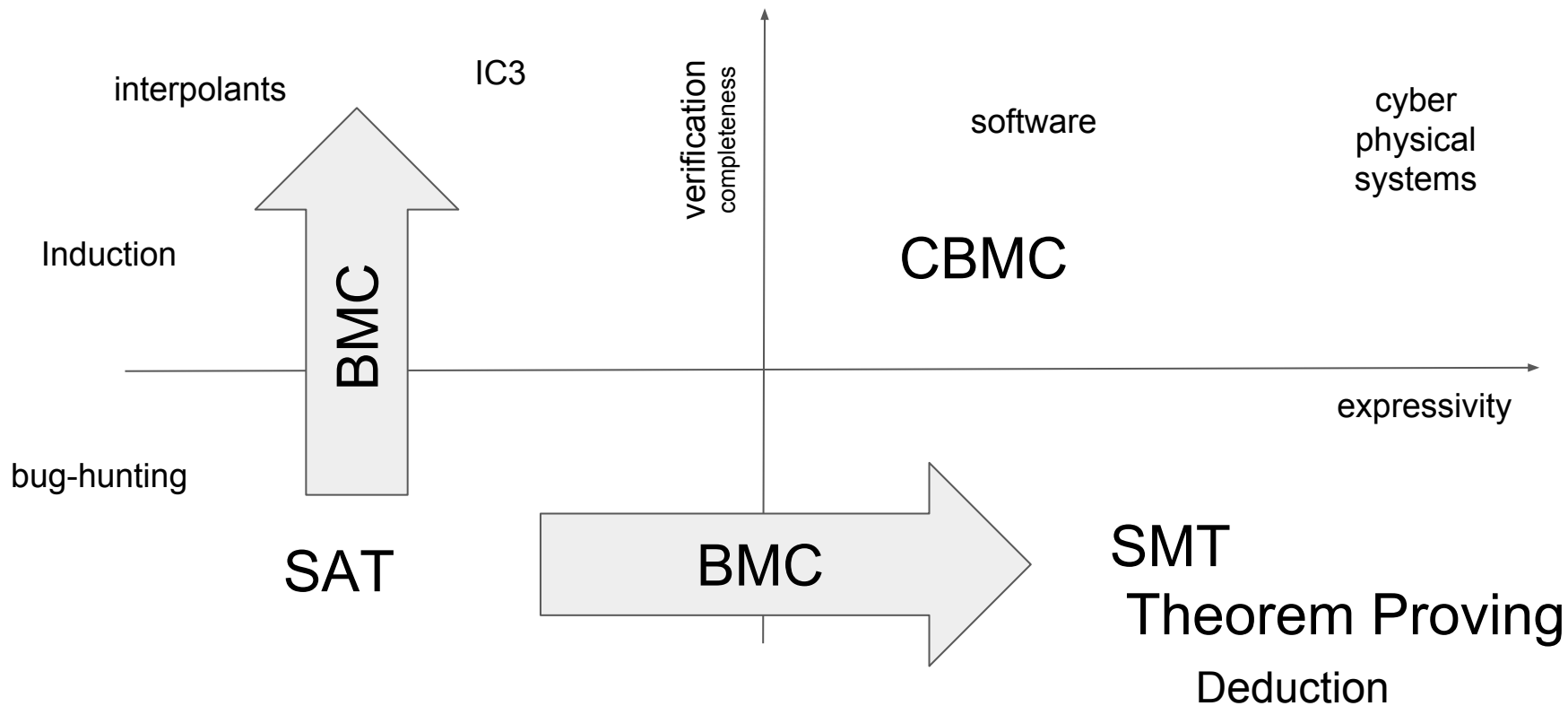


- widespread use in industry (EDA)
  - industry embraced bounding part immediately
  - original *industrial* reservations: using SAT vs ATPG
  - original *academic* reservations: incompleteness?
- BMC relies on efficient SAT (SMT) solving
  - breakthroughs in SAT: CDCL '96, VSIDS '01, ...
  - encouraged investment in SAT / SMT research
- extensions to *completeness*
  - diameter checking,  $k$ -induction, interpolation
  - SAT based model checking *without* unrolling: IC3
- extensions to *non-boolean* domains
  - infinite state systems
  - bounding reduces complexity & increases decidability
  - software

→ CBMC



# BMC as Enabler



# BMC for Software

- 2001: *Edmund Clarke* hired *Daniel Kroening* as Post-Doc  
***Use SAT for Software Model Checking!*** (expertise on Theorem Proving)
- 2002: First paper at a local Pittsburgh workshop: “Application Specific Higher Order Logic Theorem Proving”, featuring a “combination of Hoare Triple and Gentzen sequent”
- 2003: Paper on CBMC for HW/SW co-verification, first at ASP-DAC, then DAC
- 2004: Tool paper
- 2008: FShell Paper by Michael Tautschnig, while student in Helmut Veith’s group
- 2011: *Daniel Kroening* hired *Michael Tautschnig* as Post-Doc
- 2018: Release 5.9 -- diff to 5.8 has >300k lines

# A Tool for Checking ANSI-C Programs

Edmund Clarke, Daniel Kroening, and Flavio Lerda

Carnegie Mellon University

**Abstract.** We present a tool for the formal verification of ANSI-C programs using Bounded Model Checking (BMC). The emphasis is on usability: the tool supports almost all ANSI-C language features, including pointer constructs, dynamic memory allocation, recursion, and the `float` and `double` data types. From the perspective of the user, the verification is highly automated: the only input required is the BMC bound. The tool is integrated into a graphical user interface. This is essential for presenting long counterexample traces: the tool allows stepping through the trace in the same way a debugger allows stepping through a program.

## 1 Introduction

We present a tool that uses Bounded Model Checking to reason about low-level ANSI-C programs. There are two applications of the tool: 1) the tool checks safety properties such as the correctness of pointer constructs, and 2) the tool can compare an ANSI-C program with another design, such as a circuit given in Verilog.





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Authors Edmund Clarke, Daniel Kroening, Flavio Lerda

Publication date 2004

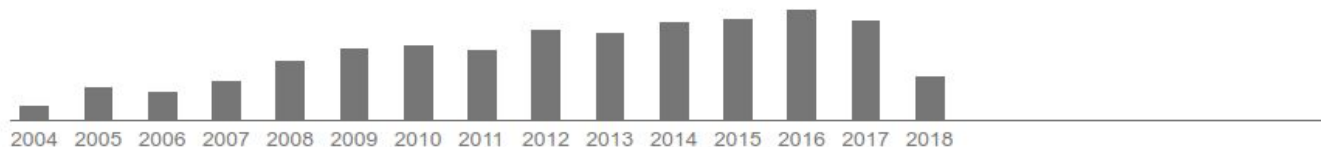
Journal Tools and Algorithms for the Construction and Analysis of Systems

Pages 168-176

Publisher Springer Berlin/Heidelberg

Description We present a tool for the formal verification of ANSI-C programs using Bounded Model Checking (BMC). The emphasis is on usability: the tool supports almost all ANSI-C language features, including pointer constructs, dynamic memory allocation, recursion, and the float and double data types. From the perspective of the user, the verification is highly automated: the only input required is the BMC bound. The tool is integrated into a graphical user interface. This is essential for presenting long counterexample traces: the tool allows stepping through the trace in the same way a debugger allows stepping through a program.

Total citations [Cited by 1272](#)



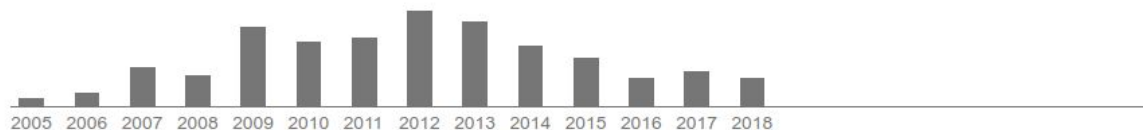
Source: Google Scholar, 28th June 2018

# CBMC

## SATABS: SAT-based predicate abstraction for ANSI-C

[PDF] from [springer.com](https://www.springer.com)

Authors	Edmund Clarke, Daniel Kroening, Natasha Sharygina, Karen Yorav
Publication date	2005/4/4
Conference	International Conference on Tools and Algorithms for the Construction and Analysis of Systems
Pages	570-574
Publisher	Springer, Berlin, Heidelberg
Description	This paper presents a model checking tool, SatAbs, that implements a predicate abstraction refinement loop. Existing software verification tools such as Slam, Blast, or Magic use decision procedures for abstraction and simulation that are limited to integers. SatAbs overcomes these limitations by using a SAT-solver. This allows the model checker to handle the semantics of the ANSI-C standard accurately. This includes a sound treatment of bit-vector overflow, and of the ANSI-C pointer arithmetic constructs.
Total citations	Cited by 336



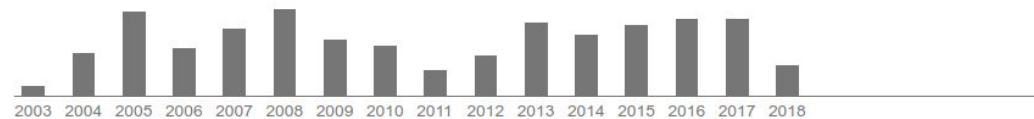
# CBMC

Source: Google Scholar, 28th June 2018

## Behavioral consistency of C and Verilog programs using bounded model checking

[PDF] from cmu.edu

Authors	Edmund Clarke, Daniel Kroening, Karen Yorav
Publication date	2003/6/2
Conference	Design Automation Conference, 2003. Proceedings
Pages	368-371
Publisher	IEEE
Description	We present an algorithm that checks behavioral consistency between an ANSI-C program and a circuit given in Verilog using Bounded Model Checking. Both the circuit and the program are unwound and translated into a formula that represents behavioral consistency. The formula is then checked using a SAT solver. We are able to translate C programs that include side effects, pointers, dynamic memory allocation, and loops with conditions that cannot be evaluated statically. We describe experimental results on various reactive circuits and programs, including a small processor given in Verilog and its Instruction Set Architecture given in ANSI-C.
Total citations	Cited by 323



# CBMC

Source: Google Scholar, 28th June 2018

# Applied Impact of CBMC

- 2011: HVC Award, recognizing the most promising academic and industrial contribution to the fields of testing and software and hardware verification from the preceding five years.
- 2014: CBMC overall winner of the Software Verification Competition (TACAS SV-COMP)
- Since 2014: BTC ships CBMC as part of their Embedded Tester product
- 2016: Diffblue Ltd spin-out founded
- 2017: CBMC best bug-finder in TACAS SV-COMP
- 2018: five of the six contestants in SV-COMP's Concurrency category use CBMC or are forks of CBMC, eight of 21 tools participating in SV-COMP use CBMC or are forks
- Industrial users include Amazon, ARM, TATA, Toyota

# Lessons

- simple but very useful ideas are highly controversial
  - hard to get accepted (literally)
  - also got many comments of the sort: *we did this before ...*
  - main points: don't be afraid, make it work, show that it works!
- in retrospective
  - complexity classification considerations (so more theory)  
might have been useful since we tried to use SAT for symbolic model  
checking without taking Savitch's theorem into account
  - but might also have prevented us going along that route ...



# SAT Based Model Checking

- BMC
- $k$ -induction
- Abstractions / CEGAR
- Interpolation
- IC3

Armin Biere, Daniel Kröning  
*SAT Based Model Checking*  
Handbook of Model Checking